

Compiler course

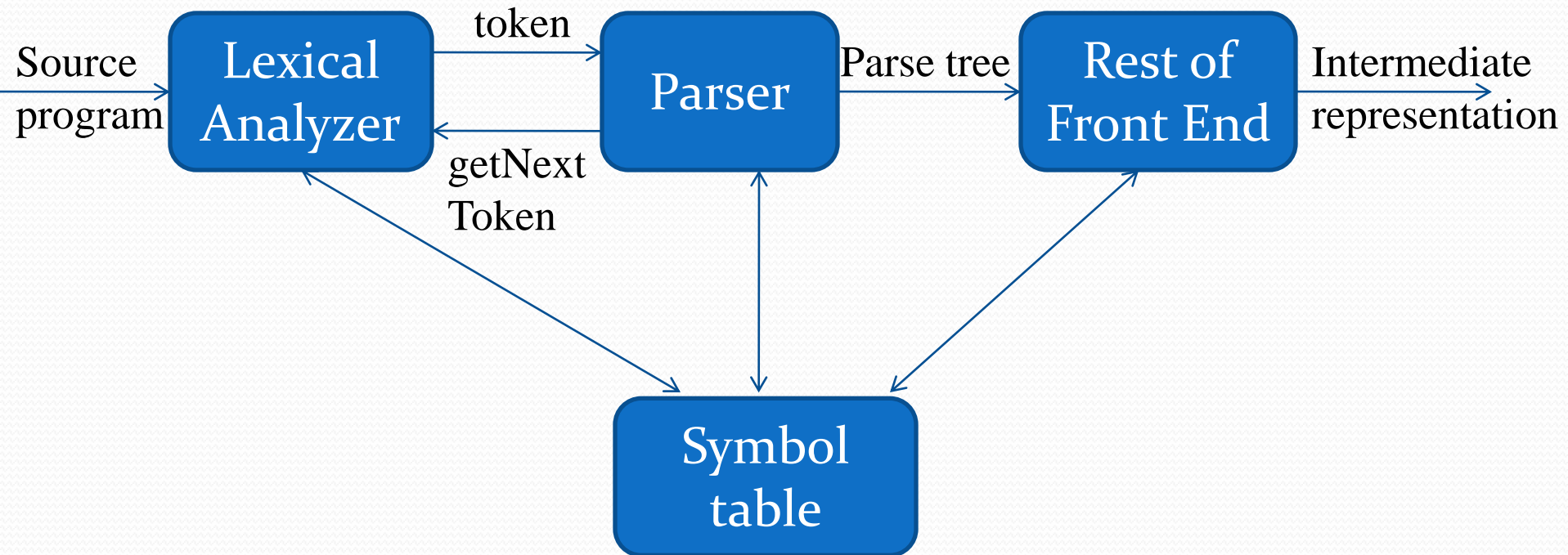
Chapter 4

Syntax Analysis

Outline

- Role of parser
- Context free grammars
- Top down parsing
- Bottom up parsing
- Parser generators

The role of parser



Uses of grammars

$$E \rightarrow E + T \mid T$$
$$T \rightarrow T * F \mid F$$
$$F \rightarrow (E) \mid \mathbf{id}$$
$$E \rightarrow TE'$$
$$E' \rightarrow +TE' \mid \varepsilon$$
$$T \rightarrow FT'$$
$$T' \rightarrow *FT' \mid \varepsilon$$
$$F \rightarrow (E) \mid \mathbf{id}$$

Error handling

- Common programming errors
 - Lexical errors
 - Syntactic errors
 - Semantic errors
 - Lexical errors
- Error handler goals
 - Report the presence of errors clearly and accurately
 - Recover from each error quickly enough to detect subsequent errors
 - Add minimal overhead to the processing of correct progrms

Error-recover strategies

- Panic mode recovery
 - Discard input symbol one at a time until one of designated set of synchronization tokens is found
- Phrase level recovery
 - Replacing a prefix of remaining input by some string that allows the parser to continue
- Error productions
 - Augment the grammar with productions that generate the erroneous constructs
- Global correction
 - Choosing minimal sequence of changes to obtain a globally least-cost correction

Context free grammars

- Terminals
- Nonterminals
- Start symbol
- productions

expression \rightarrow expression + term

expression \rightarrow expression – term

expression \rightarrow term

term \rightarrow term * factor

term \rightarrow term / factor

term \rightarrow factor

factor \rightarrow (expression)

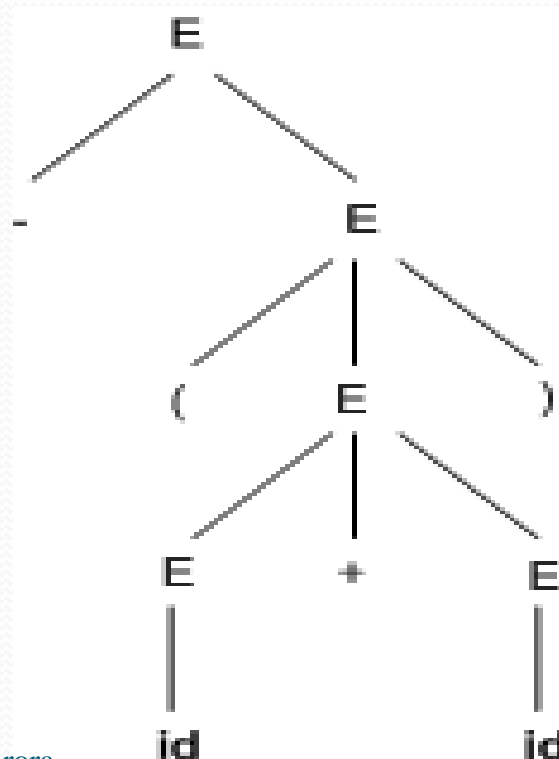
factor \rightarrow **id**

Derivations

- Productions are treated as rewriting rules to generate a string
- Rightmost and leftmost derivations
 - $E \rightarrow E + E \mid E * E \mid -E \mid (E) \mid \mathbf{id}$
 - Derivations for $\mathbf{-(id+id)}$
 - $E \Rightarrow -E \Rightarrow -(E) \Rightarrow -(E+E) \Rightarrow -(\mathbf{id}+E) \Rightarrow -(\mathbf{id}+\mathbf{id})$

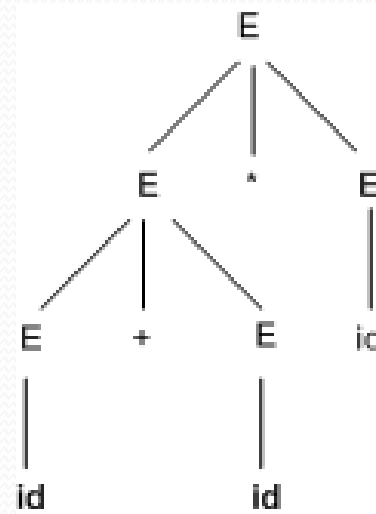
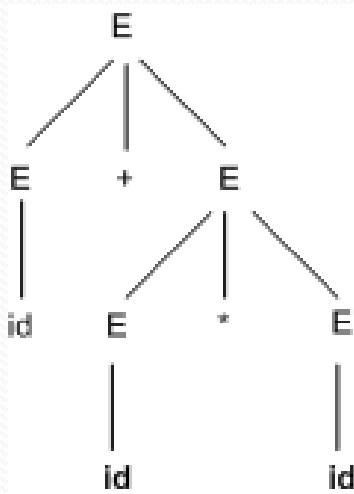
Parse trees

- **-(id+id)**
- $E \Rightarrow -E \Rightarrow -(E) \Rightarrow -(E+E) \Rightarrow -(\text{id}+E) \Rightarrow -(\text{id}+\text{id})$



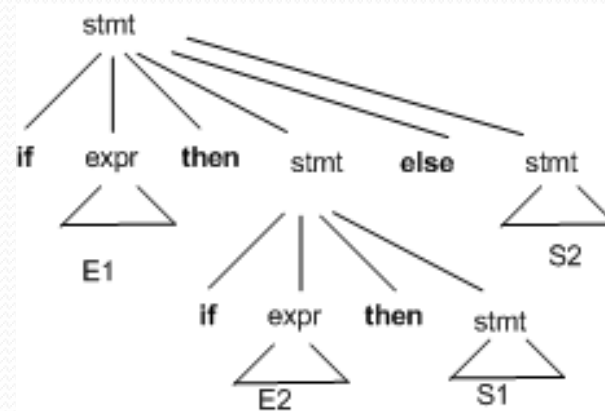
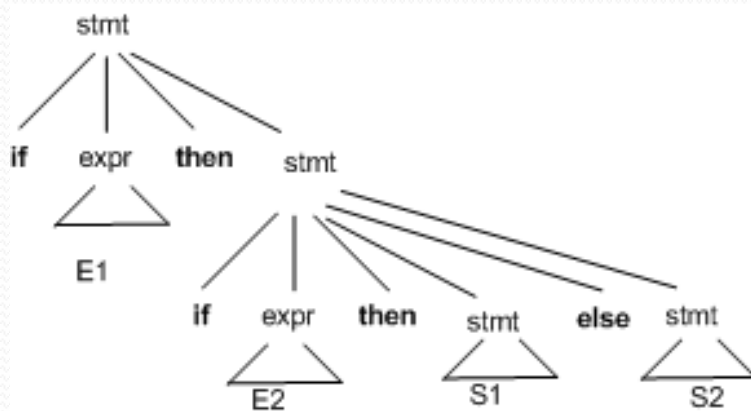
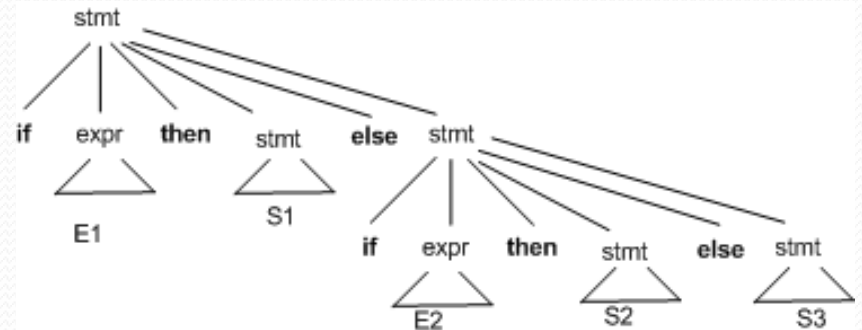
Ambiguity

- For some strings there exist more than one parse tree
- Or more than one leftmost derivation
- Or more than one rightmost derivation
- Example: $\text{id} + \text{id} * \text{id}$



Elimination of ambiguity

stmt \rightarrow If expr then stmt
| If expr then stmt else stmt
| other



Elimination of ambiguity (cont.)

- Idea:
 - A statement appearing between a **then** and an **else** must be matched

```
stmt  →  matched_stmt
      |  open_stmt

matched_stmt → If expr then matched_stmt else matched_stmt
            |  other

open_stmt  →  If expr then stmt
            |  If expr then matched_stmt else open_stmt
```

Elimination of left recursion

- A grammar is left recursive if it has a non-terminal A such that there is a derivation $A \xRightarrow{+} A \alpha$
- Top down parsing methods cant handle left-recursive grammars
- A simple rule for direct left recursion elimination:
 - For a rule like:
 - $A \rightarrow A \alpha \mid \beta$
 - We may replace it with
 - $A \rightarrow \beta A'$
 - $A' \rightarrow \alpha A' \mid \epsilon$

Left recursion elimination (cont.)

- There are cases like following
 - $S \rightarrow Aa \mid b$
 - $A \rightarrow Ac \mid Sd \mid \varepsilon$
- Left recursion elimination algorithm:
 - Arrange the nonterminals in some order A_1, A_2, \dots, A_n .
 - For (each i from 1 to n) {
 - For (each j from 1 to $i-1$) {
 - Replace each production of the form $A_i \rightarrow A_j \gamma$ by the production $A_i \rightarrow \delta_1 \gamma \mid \delta_2 \gamma \mid \dots \mid \delta_k \gamma$ where $A_j \rightarrow \delta_1 \mid \delta_2 \mid \dots \mid \delta_k$ are all current A_j productions
 - }
 - Eliminate left recursion among the A_i -productions
 - }

Left factoring

- Left factoring is a grammar transformation that is useful for producing a grammar suitable for predictive or top-down parsing.
- Consider following grammar:
 - $\text{Stmt} \rightarrow \text{if expr then stmt else stmt}$
 - $\quad \quad \quad | \text{if expr then stmt}$
- On seeing input **if** it is not clear for the parser which production to use
- We can easily perform left factoring:
 - If we have $A \rightarrow \alpha \beta_1 \mid \alpha \beta_2$ then we replace it with
 - $A \rightarrow \alpha A'$
 - $A' \rightarrow \beta_1 \mid \beta_2$

Left factoring (cont.)

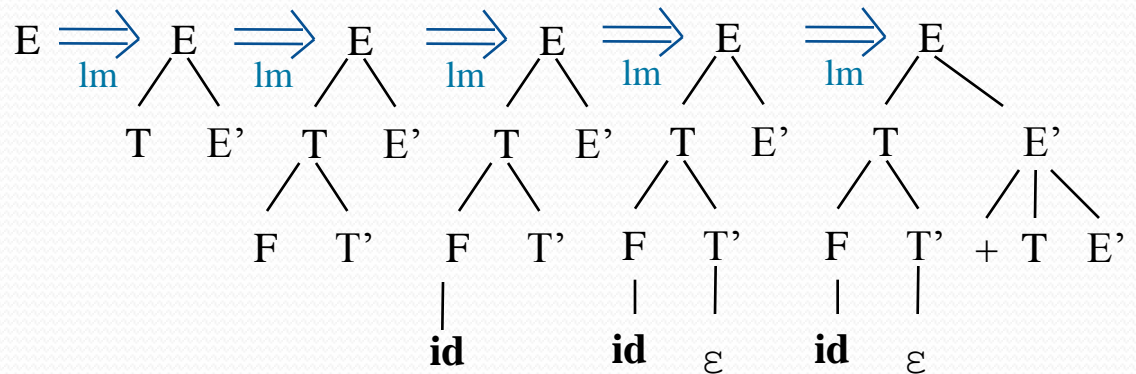
- Algorithm
 - For each non-terminal A , find the longest prefix α common to two or more of its alternatives. If $\alpha \neq \epsilon$, then replace all of A -productions $A \rightarrow \alpha \beta_1 \mid \alpha \beta_2 \mid \dots \mid \alpha \beta_n \mid \gamma$ by
 - $A \rightarrow \alpha A' \mid \gamma$
 - $A' \rightarrow \beta_1 \mid \beta_2 \mid \dots \mid \beta_n$
- Example:
 - $S \rightarrow I E t S \mid i E t S e S \mid a$
 - $E \rightarrow b$

Top Down Parsing

Introduction

- A Top-down parser tries to create a parse tree from the root towards the leafs scanning input from left to right
- It can be also viewed as finding a leftmost derivation for an input string
- Example: $\text{id}+\text{id}*\text{id}$

$E \rightarrow TE'$
 $E' \rightarrow +TE' \mid \varepsilon$
 $T \rightarrow FT'$
 $T' \rightarrow *FT' \mid \varepsilon$
 $F \rightarrow (E) \mid \text{id}$



Recursive descent parsing

- Consists of a set of procedures, one for each nonterminal
- Execution begins with the procedure for start symbol
- A typical procedure for a non-terminal

```
void A() {  
    choose an A-production,  $A \rightarrow X_1X_2..X_k$   
    for (i=1 to k) {  
        if ( $X_i$  is a nonterminal  
            call procedure  $X_i()$ ;  
        else if ( $X_i$  equals the current input symbol a)  
            advance the input to the next symbol;  
        else /* an error has occurred */  
    }  
}
```

Recursive descent parsing (cont)

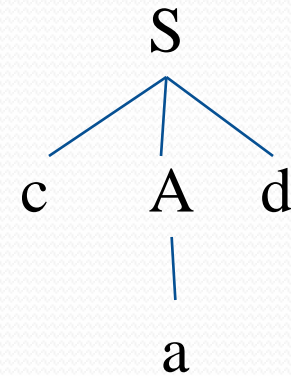
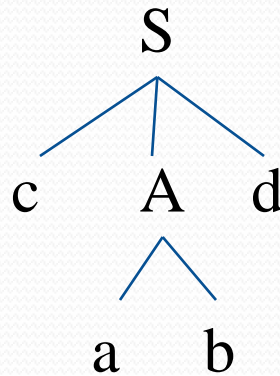
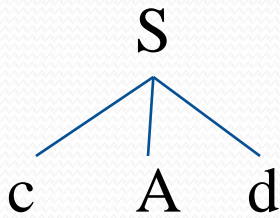
- General recursive descent may require backtracking
- The previous code needs to be modified to allow backtracking
- In general form it can't choose an A-production easily.
- So we need to try all alternatives
- If one failed the input pointer needs to be reset and another alternative should be tried
- Recursive descent parsers can't be used for left-recursive grammars

Example

$S \rightarrow cAd$

$A \rightarrow ab \mid a$

Input: cad



First and Follow

- $\text{First}()$ is set of terminals that begins strings derived from
- If $\alpha \xRightarrow{*} \varepsilon$ then ε is also in $\text{First}(\varepsilon)$
- In predictive parsing when we have $A \rightarrow \alpha \mid \beta$, if $\text{First}(\alpha)$ and $\text{First}(\beta)$ are disjoint sets then we can select appropriate A-production by looking at the next input
- $\text{Follow}(A)$, for any nonterminal A, is set of terminals a that can appear immediately after A in some sentential form
 - If we have $S \xRightarrow{*} \alpha A a \beta$ for some α and β then a is in $\text{Follow}(A)$
- If A can be the rightmost symbol in some sentential form, then $\$$ is in $\text{Follow}(A)$

Computing First

- To compute $\text{First}(X)$ for all grammar symbols X , apply following rules until no more terminals or ϵ can be added to any First set:
 1. If X is a terminal then $\text{First}(X) = \{X\}$.
 2. If X is a nonterminal and $X \rightarrow Y_1 Y_2 \dots Y_k$ is a production for some $k \geq 1$, then place a in $\text{First}(X)$ if for some i a is in $\text{First}(Y_i)$ and ϵ is in all of $\text{First}(Y_1), \dots, \text{First}(Y_{i-1})$ that is $Y_1 \dots Y_{i-1} \xRightarrow{*} \epsilon$. if ϵ is in $\text{First}(Y_j)$ for $j=1, \dots, k$ then add ϵ to $\text{First}(X)$.
 3. If $X \rightarrow \epsilon$ is a production then add ϵ to $\text{First}(X)$
- Example!

Computing follow

- To compute $\text{First}(A)$ for all nonterminals A , apply following rules until nothing can be added to any follow set:
 1. Place $\$$ in $\text{Follow}(S)$ where S is the start symbol
 2. If there is a production $A \rightarrow \alpha B \beta$ then everything in $\text{First}(\beta)$ except ϵ is in $\text{Follow}(B)$.
 3. If there is a production $A \rightarrow B$ or a production $A \rightarrow \alpha B \beta$ where $\text{First}(\beta)$ contains ϵ , then everything in $\text{Follow}(A)$ is in $\text{Follow}(B)$
- Example!

LL(1) Grammars

- Predictive parsers are those recursive descent parsers needing no backtracking
- Grammars for which we can create predictive parsers are called LL(1)
 - The first L means scanning input from left to right
 - The second L means leftmost derivation
 - And 1 stands for using one input symbol for lookahead
- A grammar G is LL(1) if and only if whenever $A \rightarrow \alpha \mid \beta$ are two distinct productions of G , the following conditions hold:
 - For no terminal a do α and β both derive strings beginning with a
 - At most one of α or β can derive empty string
 - If $\alpha \Rightarrow \varepsilon$ then β does not derive any string beginning with a terminal in $\text{Follow}(A)$.

Construction of predictive parsing table

- For each production $A \rightarrow \alpha$ in grammar do the following:
 1. For each terminal a in $\text{First}(\alpha)$ add $A \rightarrow$ in $M[A, a]$
 2. If ϵ is in $\text{First}(\alpha)$, then for each terminal b in $\text{Follow}(A)$ add $A \rightarrow \epsilon$ to $M[A, b]$. If ϵ is in $\text{First}(\alpha)$ and $\$$ is in $\text{Follow}(A)$, add $A \rightarrow \epsilon$ to $M[A, \$]$ as well
- If after performing the above, there is no production in $M[A, a]$ then set $M[A, a]$ to error

Example

$E \rightarrow TE'$

$E' \rightarrow +TE' \mid \varepsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \varepsilon$

$F \rightarrow (E) \mid \mathbf{id}$

	First	Follow
F	{(,id}	{+, *,), \$}
T	{(,id}	{+,), \$}
E	{(,id}	{), \$}
E'	{+,ε}	{), \$}
T'	{*,ε}	{+,), \$}

Non - terminal	Input Symbol					
	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow \mathbf{id}$			$F \rightarrow (E)$		

Another example

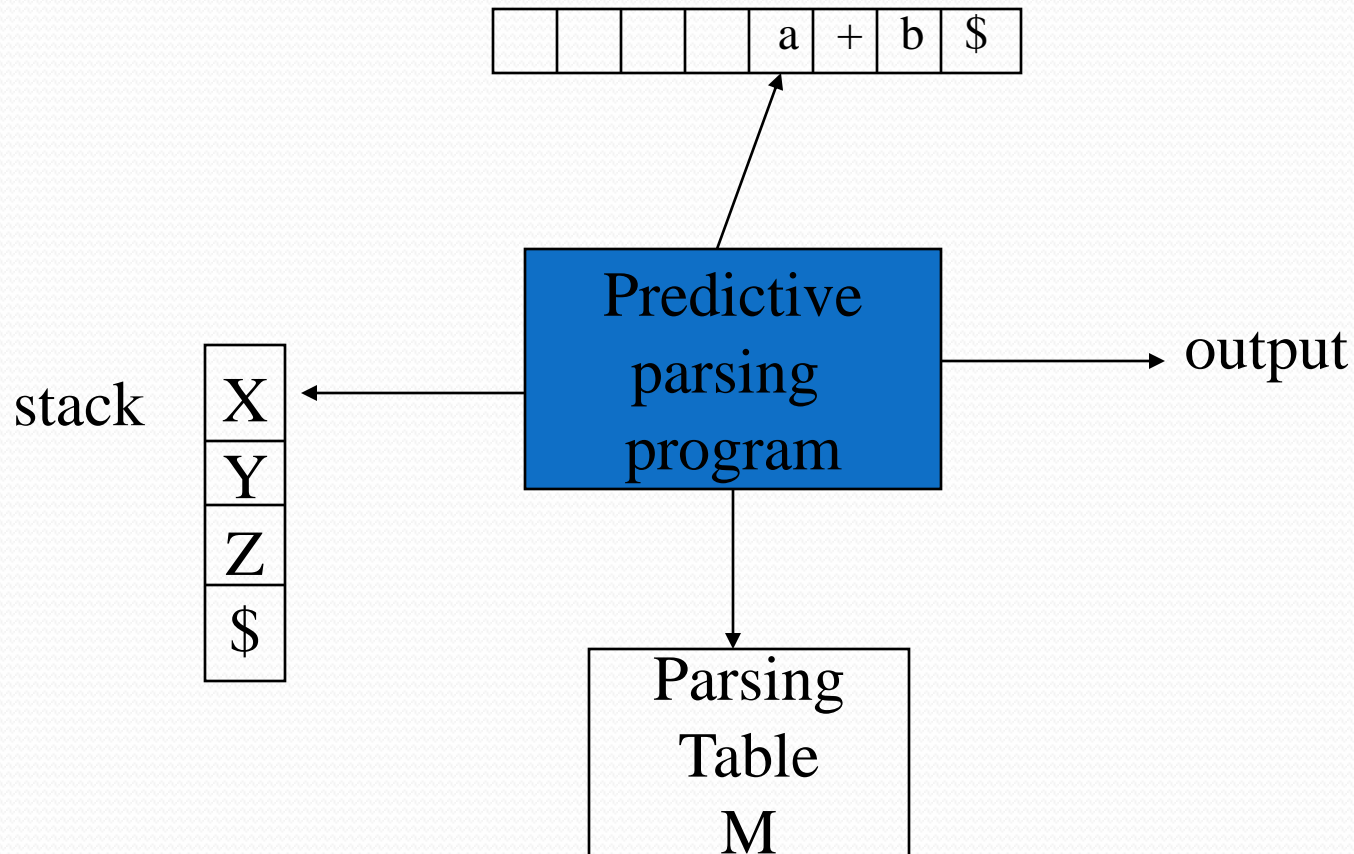
$S \rightarrow iEtSS' \mid a$

$S' \rightarrow eS \mid \epsilon$

$E \rightarrow b$

Non - terminal	Input Symbol					
	a	b	e	i	t	\$
S	$S \rightarrow a$			$S \rightarrow iEtSS'$		
S'			$S' \rightarrow \epsilon$ $S' \rightarrow eS$			$S' \rightarrow \epsilon$
E		$E \rightarrow b$				

Non-recursive predicting parsing



Predictive parsing algorithm

Set ip point to the first symbol of w;

Set X to the top stack symbol;

While (X<>\$) { /* stack is not empty */

 if (X is a) pop the stack and advance ip;

 else if (X is a terminal) error();

 else if (M[X,a] is an error entry) error();

 else if (M[X,a] = X->Y₁Y₂..Y_k) {

 output the production X->Y₁Y₂..Y_k;

 pop the stack;

 push Y_k,...,Y₂,Y₁ on to the stack with Y₁ on top;

 }

 set X to the top stack symbol;

}

Example

- $\text{id+id*id\$}$

Matched	Stack	Input	Action
	E\$	$\text{id+id*id\$}$	

Error recovery in predictive parsing

- Panic mode
 - Place all symbols in $\text{Follow}(A)$ into synchronization set for nonterminal A : skip tokens until an element of $\text{Follow}(A)$ is seen and pop A from stack.
 - Add to the synchronization set of lower level construct the symbols that begin higher level constructs
 - Add symbols in $\text{First}(A)$ to the synchronization set of nonterminal A
 - If a nonterminal can generate the empty string then the production deriving can be used as a default
 - If a terminal on top of the stack cannot be matched, pop the terminal, issue a message saying that the terminal was insterted

Example

Non - terminal	Input Symbol					
	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$	synch	synch
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$	synch		$T \rightarrow FT'$	synch	synch
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$	synch	synch	$F \rightarrow (E)$	synch	synch

Stack	Input	Action
E\$)id*+id\$	Error, Skip)
E\$	id*+id\$	id is in First(E)
TE'\$	id*+id\$	
FT'E'\$	id*+id\$	
idT'E'\$	id*+id\$	
T'E'\$	*+id\$	
*FT'E'\$	*+id\$	
FT'E'\$	+id\$	Error, M[F,+]=synch
T'E'\$	+id\$	F has been popped

Bottom-up Parsing

Introduction

- Constructs parse tree for an input string beginning at the leaves (the bottom) and working towards the root (the top)
- Example: $\text{id} * \text{id}$

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow (E) \mid \text{id}$

$\text{id} * \text{id}$

$F * \text{id}$

$T * \text{id}$

$T * F$

F

E

|

|

|

|

^

|

id

F

F

id

$T * F$

F

|

|

|

|

^

id

id

F

id

$T * F$

id

|

|

|

id

F

id

|

id

Shift-reduce parser

- The general idea is to shift some symbols of input to the stack until a reduction can be applied
- At each reduction step, a specific substring matching the body of a production is replaced by the nonterminal at the head of the production
- The key decisions during bottom-up parsing are about when to reduce and about what production to apply
- A reduction is a reverse of a step in a derivation
- The goal of a bottom-up parser is to construct a derivation in reverse:

- $E \Rightarrow T \Rightarrow T * F \Rightarrow T * id \Rightarrow F * id \Rightarrow id * id$

Handle pruning

- A Handle is a substring that matches the body of a production and whose reduction represents one step along the reverse of a rightmost derivation

Right sentential form	Handle	Reducing production
id*id	id	$F \rightarrow id$
F*id	F	$T \rightarrow F$
T*id	id	$F \rightarrow id$
T*F	T*F	$E \rightarrow T*F$

Shift reduce parsing

- A stack is used to hold grammar symbols
- Handle always appear on top of the stack
- Initial configuration:

Stack	Input
\$	w\$

- Acceptance configuration

Stack	Input
\$S	\$

Shift reduce parsing (cont.)

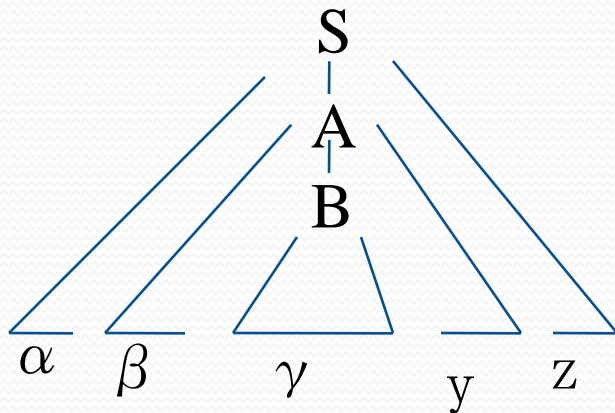
- Basic operations:

- Shift
- Reduce
- Accept
- Error

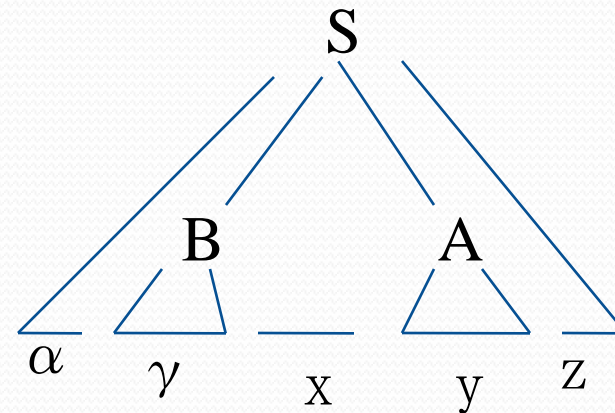
- Example: $id * id$

Stack	Input	Action
\$	$id * id \$$	shift
$\$id$	$* id \$$	reduce by $F \rightarrow id$
$\$F$	$* id \$$	reduce by $T \rightarrow F$
$\$T$	$* id \$$	shift
$\$T*$	$id \$$	shift
$\$T * id$	$\$$	reduce by $F \rightarrow id$
$\$T * F$	$\$$	reduce by $T \rightarrow T * F$
$\$T$	$\$$	reduce by $E \rightarrow T$
$\$E$	$\$$	accept

Handle will appear on top of the stack



Stack	Input
$\$ \alpha \beta \gamma$	$yz\$$
$\$ \alpha \beta B$	$yz\$$
$\$ \alpha \beta By$	$z\$$



Stack	Input
$\$ \alpha \gamma$	$xyz\$$
$\$ \alpha Bxy$	$z\$$

Conflicts during shift reduce parsing

- Two kind of conflicts
 - Shift/reduce conflict
 - Reduce/reduce conflict
- Example:

```
stmt  →  if expr then stmt
        |  if expr then stmt else stmt
        |  other
```

Stack

... if expr then stmt

Input

else ...\$

Reduce/reduce conflict

stmt -> id(parameter_list)

stmt -> expr:=expr

parameter_list->parameter_list, parameter

parameter_list->parameter

parameter->id

expr->id(expr_list)

expr->id

expr_list->expr_list, expr

expr_list->expr

Stack

... id(id

Input

,id) ...\$

LR Parsing

- The most prevalent type of bottom-up parsers
- LR(k), mostly interested on parsers with $k \leq 1$
- Why LR parsers?
 - Table driven
 - Can be constructed to recognize all programming language constructs
 - Most general non-backtracking shift-reduce parsing method
 - Can detect a syntactic error as soon as it is possible to do so
 - Class of grammars for which we can construct LR parsers are superset of those which we can construct LL parsers

States of an LR parser

- States represent set of items
- An LR(o) item of G is a production of G with the dot at some position of the body:
 - For $A \rightarrow XYZ$ we have following items
 - $A \rightarrow .XYZ$
 - $A \rightarrow X.YZ$
 - $A \rightarrow XY.Z$
 - $A \rightarrow XYZ.$
 - In a state having $A \rightarrow .XYZ$ we hope to see a string derivable from XYZ next on the input.
 - What about $A \rightarrow X.YZ$?

Constructing canonical LR(0) item sets

- Augmented grammar:
 - G with addition of a production: $S' \rightarrow S$
- Closure of item sets:
 - If I is a set of items, $\text{closure}(I)$ is a set of items constructed from I by the following rules:
 - Add every item in I to $\text{closure}(I)$
 - If $A \rightarrow \alpha.B\beta$ is in $\text{closure}(I)$ and $B \rightarrow \gamma$ is a production then add the item $B \rightarrow \gamma$ to $\text{closure}(I)$.

- Example:

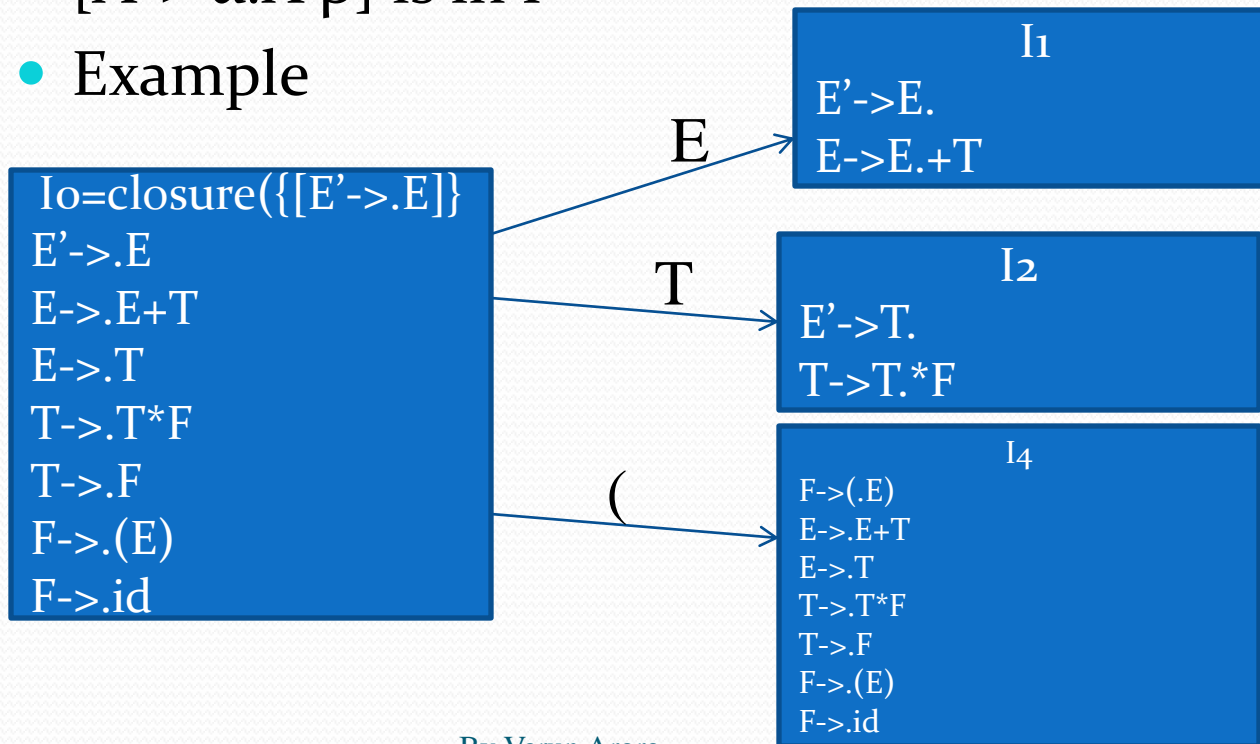
$E' \rightarrow E$
 $E \rightarrow E + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow (E) \mid \mathbf{id}$

$I_0 = \text{closure}(\{[E' \rightarrow \cdot E]\})$

$E' \rightarrow \cdot E$
 $E \rightarrow \cdot E + T$
 $E \rightarrow \cdot T$
 $T \rightarrow \cdot T * F$
 $T \rightarrow \cdot F$
 $F \rightarrow \cdot (E)$
 $F \rightarrow \cdot \mathbf{id}$

Constructing canonical LR(0) item sets (cont.)

- Goto (I, X) where I is an item set and X is a grammar symbol is closure of set of all items $[A \rightarrow \alpha X \beta]$ where $[A \rightarrow \alpha.X \beta]$ is in I
- Example



Closure algorithm

SetOfItems CLOSURE(I) {

$J = I$;

 repeat

 for (each item $A \rightarrow \alpha.B\beta$ in J)

 for (each production $B \rightarrow \gamma$ of G)

 if ($B \rightarrow \gamma$ is not in J)

 add $B \rightarrow \gamma$ to J ;

 until no more items are added to J on one round;

 return J ;

GOTO algorithm

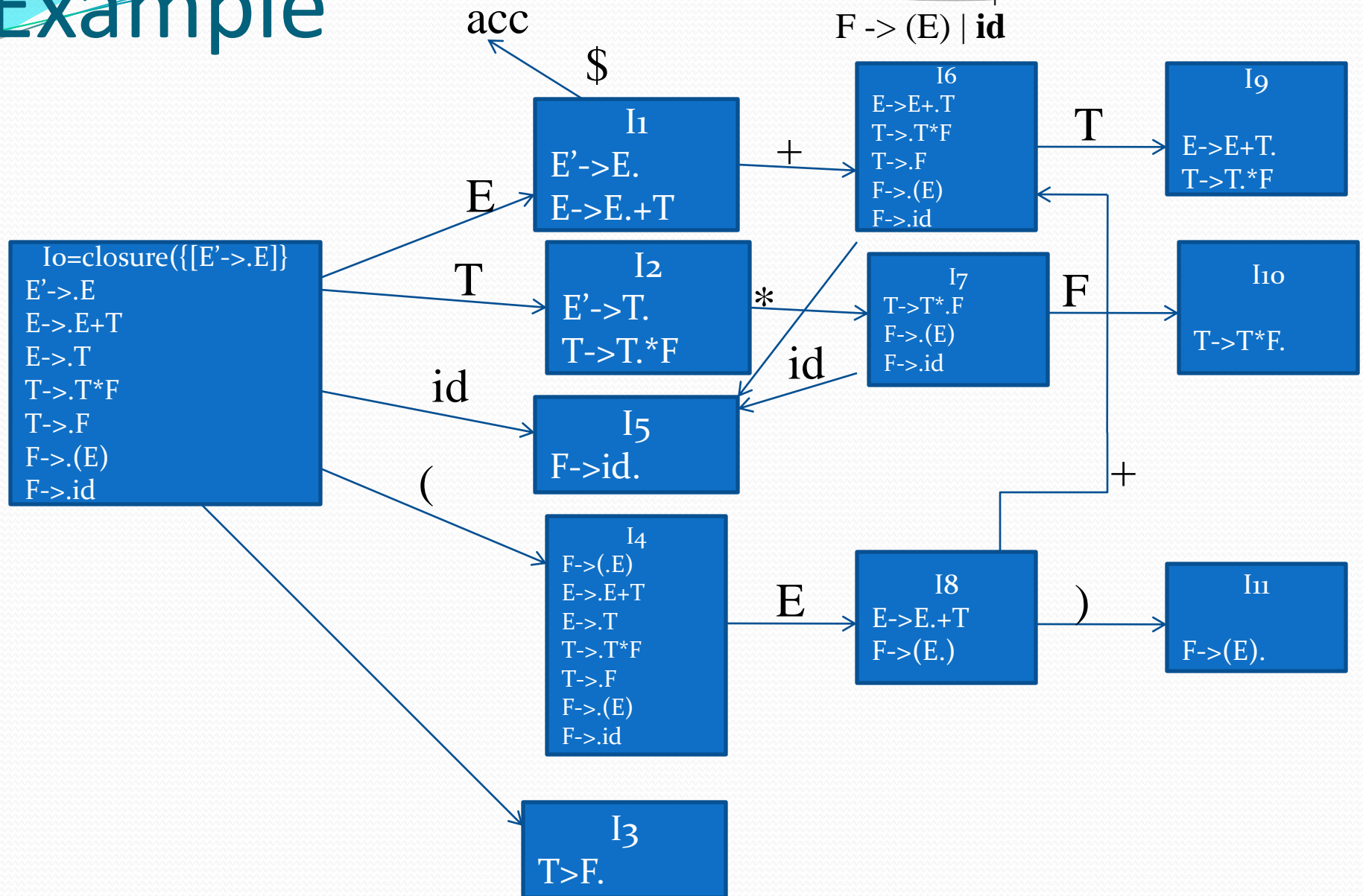
```
SetOfItems GOTO(I,X) {  
    J=empty;  
    if ( $A \rightarrow \alpha.X \beta$  is in I)  
        add CLOSURE( $A \rightarrow \alpha.X. \beta$ ) to J;  
    return J;  
}
```


Canonical LR(0) items

```
Void items( $G'$ ) {  
     $C = \text{CLOSURE}(\{[S' \rightarrow \cdot S]\});$   
    repeat  
        for (each set of items  $I$  in  $C$ )  
            for (each grammar symbol  $X$ )  
                if ( $\text{GOTO}(I, X)$  is not empty and not in  $C$ )  
                    add  $\text{GOTO}(I, X)$  to  $C$ ;  
    until no new set of items are added to  $C$  on a round;  
}
```

Example

$E' \rightarrow E$
 $E \rightarrow E + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow (E) \mid id$

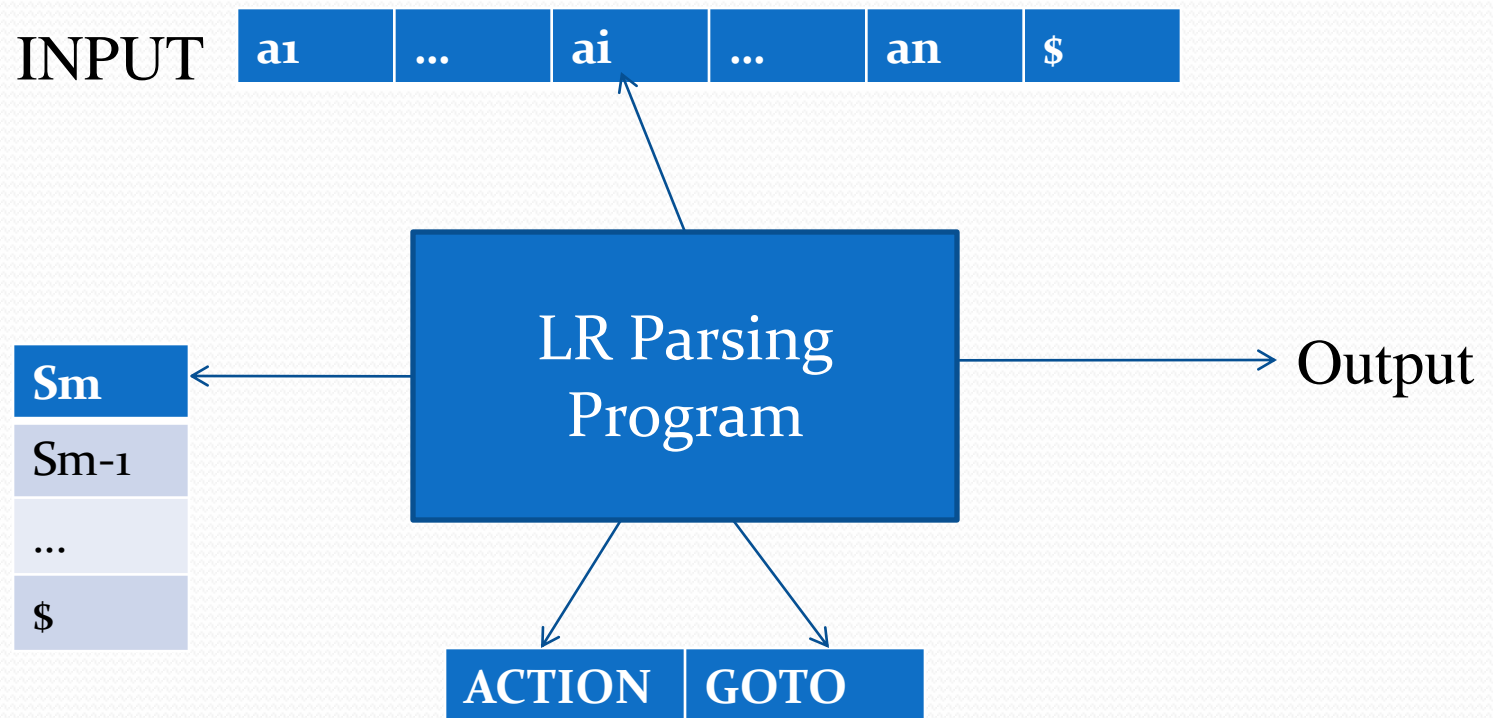


Use of LR(0) automaton

- Example: id^*id

Line	Stack	Symbols	Input	Action
(1)	0	\$	id*id\$	Shift to 5
(2)	05	\$id	*id\$	Reduce by $F \rightarrow \text{id}$
(3)	03	\$F	*id\$	Reduce by $T \rightarrow F$
(4)	02	\$T	*id\$	Shift to 7
(5)	027	\$T*	id\$	Shift to 5
(6)	0275	\$T*id	\$	Reduce by $F \rightarrow \text{id}$
(7)	02710	\$T*F	\$	Reduce by $T \rightarrow T*F$
(8)	02	\$T	\$	Reduce by $E \rightarrow T$
(9)	01	\$E	\$	accept

LR-Parsing model



LR parsing algorithm

```
let a be the first symbol of w$;
while(1) { /*repeat forever */
    let s be the state on top of the stack;
    if (ACTION[s,a] = shift t) {
        push t onto the stack;
        let a be the next input symbol;
    } else if (ACTION[s,a] = reduce A-> $\beta$ ) {
        pop  $|\beta|$  symbols of the stack;
        let state t now be on top of the stack;
        push GOTO[t,A] onto the stack;
        output the production A-> $\beta$ ;
    } else if (ACTION[s,a]=accept) break; /* parsing is done */
    else call error-recovery routine;
}
```

Example

(0) $E' \rightarrow E$

(1) $E \rightarrow E + T$

(2) $E \rightarrow T$

(3) $T \rightarrow T * F$

(4) $T \rightarrow F$

(5) $F \rightarrow (E)$

(6) $F \rightarrow id$

id*id+id?

STATE	ACTION						GOTO		
	id	+	*	()	\$	E	T	F
0	S ₅			S ₄			1	2	3
1		S ₆				Acc			
2		R ₂	S ₇		R ₂	R ₂			
3		R ₄	R ₇		R ₄	R ₄			
4	S ₅			S ₄			8	2	3
5		R ₆	R ₆		R ₆	R ₆			
6	S ₅			S ₄				9	3
7	S ₅			S ₄					10
8		S ₆			S ₁₁				
9		R ₁	S ₇		R ₁	R ₁			
10		R ₃	R ₃		R ₃	R ₃			
11		R ₅	R ₅		R ₅	R ₅			

Line	Stack	Symbols	Input	Action
(1)	o		id*id+id\$	Shift to 5
(2)	o5	id	*id+id\$	Reduce by $F \rightarrow id$
(3)	o3	F	*id+id\$	Reduce by $T \rightarrow F$
(4)	o2	T	*id+id\$	Shift to 7
(5)	o27	T*	id+id\$	Shift to 5
(6)	o275	T*id	+id\$	Reduce by $F \rightarrow id$
(7)	o2710	T*F	+id\$	Reduce by $T \rightarrow T*F$
(8)	o2	T	+id\$	Reduce by $E \rightarrow T$
(9)	o1	E	+id\$	Shift
(10)	o16	E+	id\$	Shift
(11)	o165	E+id	\$	Reduce by $F \rightarrow id$
(12)	o163	E+F	\$	Reduce by $T \rightarrow F$
(13)	o169	E+T'	\$	Reduce by $E \rightarrow E+T$
(14)	o1	E	\$	accept

Constructing SLR parsing table

- Method

- Construct $C = \{I_0, I_1, \dots, I_n\}$, the collection of LR(o) items for G'
- State i is constructed from state I_i :
 - If $[A \rightarrow \alpha.a\beta]$ is in I_i and $\text{Goto}(I_i, a) = I_j$, then set $\text{ACTION}[i, a]$ to “shift j ”
 - If $[A \rightarrow \alpha.]$ is in I_i , then set $\text{ACTION}[i, a]$ to “reduce $A \rightarrow \alpha$ ” for all a in $\text{follow}(A)$
 - If $\{S' \rightarrow .S\}$ is in I_i , then set $\text{ACTION}[i, \$]$ to “Accept”
- If any conflicts appears then we say that the grammar is not $\text{SLR}(1)$.
- If $\text{GOTO}(I_i, A) = I_j$ then $\text{GOTO}[i, A] = j$
- All entries not defined by above rules are made “error”
- The initial state of the parser is the one constructed from the set of items containing $[S' \rightarrow .S]$

Example grammar which is not SLR(1)

$S \rightarrow L=R \mid R$

$L \rightarrow *R \mid \text{id}$

$R \rightarrow L$

I0
 $S' \rightarrow .S$
 $S \rightarrow .L=R$
 $S \rightarrow .R$
 $L \rightarrow .*R \mid$
 $L \rightarrow .\text{id}$
 $R \rightarrow .L$

I1
 $S' \rightarrow S.$

I2
 $S \rightarrow L.=R$
 $R \rightarrow L.$

I3
 $S \rightarrow R.$

I4
 $L \rightarrow *.R$
 $R \rightarrow .L$
 $L \rightarrow .*R$
 $L \rightarrow .\text{id}$

I5
 $L \rightarrow \text{id}.$

I6
 $S \rightarrow L=.R$
 $R \rightarrow .L$
 $L \rightarrow .*R$
 $L \rightarrow .\text{id}$

I7
 $L \rightarrow *R.$

I8
 $R \rightarrow L.$

I9
 $S \rightarrow L=R.$

Action

=

Shift 6

Reduce $R \rightarrow L$

More powerful LR parsers

- Canonical-LR or just LR method
 - Use lookahead symbols for items: LR(1) items
 - Results in a large collection of items
- LALR: lookaheads are introduced in LR(o) items

Canonical LR(1) items

- In LR(1) items each item is in the form: $[A \rightarrow \alpha.\beta, a]$
 - An LR(1) item $[A \rightarrow \alpha.\beta, a]$ is valid for a viable prefix γ if there is a derivation $S \xRightarrow{*} \delta A w \xRightarrow{rm} \delta \alpha \beta w$, where
 - $\Gamma = \delta \alpha$
 - Either a is the first symbol of w , or w is ϵ and a is $\$$
 - Example:
 - $S \rightarrow BB$
 - $B \rightarrow aB | b$
- $S \xRightarrow{*} aaBab \xRightarrow{rm} aaaBab$
- Item $[B \rightarrow a.B, a]$ is valid for $\gamma = aaa$ and $w = ab$

Constructing LR(1) sets of items

```
SetOfItems Closure(I) {  
    repeat  
        for (each item  $[A \rightarrow \alpha.B\beta, a]$  in I)  
            for (each production  $B \rightarrow \gamma$  in  $G'$ )  
                for (each terminal  $b$  in  $\text{First}(\beta a)$ )  
                    add  $[B \rightarrow \gamma, b]$  to set I;  
    until no more items are added to I;  
    return I;  
}
```

```
SetOfItems Goto(I, X) {  
    initialize J to be the empty set;  
    for (each item  $[A \rightarrow \alpha.X\beta, a]$  in I)  
        add item  $[A \rightarrow \alpha X.\beta, a]$  to set J;  
    return closure(J);  
}
```

```
void items( $G'$ ){  
    initialize C to  $\text{Closure}(\{[S' \rightarrow .S, \$]\})$ ;  
    repeat  
        for (each set of items I in C)  
            for (each grammar symbol X)  
                if ( $\text{Goto}(I, X)$  is not empty and not in C)  
                    add  $\text{Goto}(I, X)$  to C;  
    until no new sets of items are added to C;  
}
```

Example

$S' \rightarrow S$

$S \rightarrow CC$

$C \rightarrow cC$

$C \rightarrow d$

Canonical LR(1) parsing table

- Method

- Construct $C = \{I_0, I_1, \dots, I_n\}$, the collection of LR(1) items for G'
- State i is constructed from state I_i :
 - If $[A \rightarrow \alpha.a\beta, b]$ is in I_i and $\text{Goto}(I_i, a) = I_j$, then set $\text{ACTION}[i, a]$ to “shift j ”
 - If $[A \rightarrow \alpha., a]$ is in I_i , then set $\text{ACTION}[i, a]$ to “reduce $A \rightarrow \alpha$ ”
 - If $\{S' \rightarrow .S, \$\}$ is in I_i , then set $\text{ACTION}[i, \$]$ to “Accept”
- If any conflicts appears then we say that the grammar is not LR(1).
- If $\text{GOTO}(I_i, A) = I_j$ then $\text{GOTO}[i, A] = j$
- All entries not defined by above rules are made “error”
- The initial state of the parser is the one constructed from the set of items containing $[S' \rightarrow .S, \$]$

Example

$S' \rightarrow S$

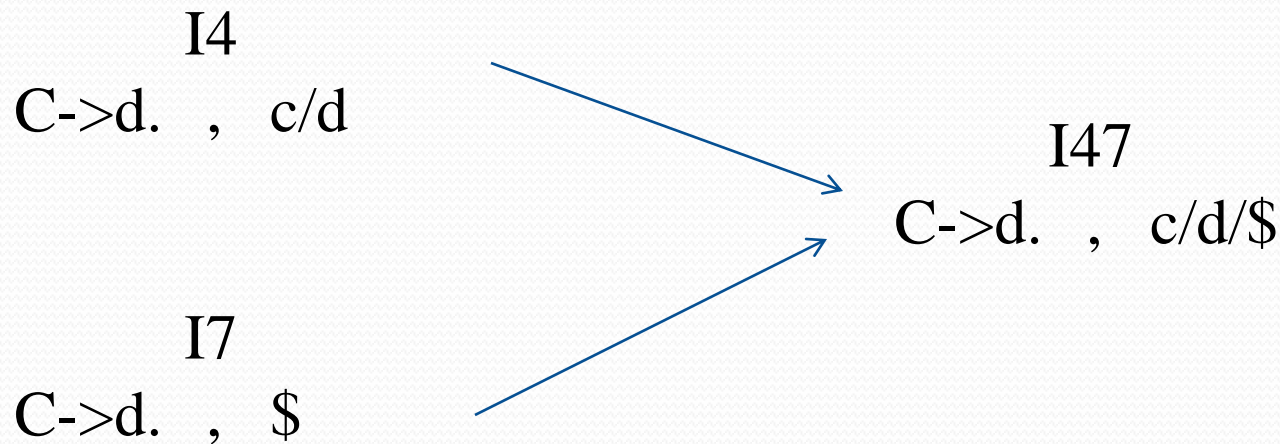
$S \rightarrow CC$

$C \rightarrow cC$

$C \rightarrow d$

LALR Parsing Table

- For the previous example we had:



- State merges can't produce Shift-Reduce conflicts. Why?
- But it may produce reduce-reduce conflict

Example of RR conflict in state merging

$S' \rightarrow S$

$S \rightarrow aAd \mid bBd \mid aBe \mid bAe$

$A \rightarrow c$

$B \rightarrow c$

An easy but space-consuming LALR table construction

- Method:
 1. Construct $C = \{I_0, I_1, \dots, I_n\}$ the collection of LR(1) items.
 2. For each core among the set of LR(1) items, find all sets having that core, and replace these sets by their union.
 3. Let $C' = \{J_0, J_1, \dots, J_m\}$ be the resulting sets. The parsing actions for state i , is constructed from J_i as before. If there is a conflict grammar is not LALR(1).
 4. If J is the union of one or more sets of LR(1) items, that is $J = I_1 \cup I_2 \dots I_k$ then the cores of $\text{Goto}(I_1, X)$, ..., $\text{Goto}(I_k, X)$ are the same and is a state like K , then we set $\text{Goto}(J, X) = K$.
- This method is not efficient, a more efficient one is discussed in the book

Compaction of LR parsing table

- Many rows of action tables are identical
 - Store those rows separately and have pointers to them from different states
 - Make lists of (terminal-symbol, action) for each state
 - Implement Goto table by having a link list for each nonterminal in the form (current state, next state)

Using ambiguous grammars

$E \rightarrow E + E$

$E \rightarrow E * E$

$E \rightarrow (E)$

$E \rightarrow id$

I0: $E' \rightarrow .E$

$E \rightarrow .E + E$

$E \rightarrow .E * E$

$E \rightarrow .(E)$

$E \rightarrow .id$

I1: $E' \rightarrow E.$

$E \rightarrow E. + E$

$E \rightarrow E. * E$

I4: $E \rightarrow E + .E$

$E \rightarrow E. + E$

$E \rightarrow E. * E$

$E \rightarrow E. (E)$

$E \rightarrow E. id$

I2: $E \rightarrow (.E)$

$E \rightarrow .E + E$

$E \rightarrow .E * E$

$E \rightarrow .(E)$

$E \rightarrow .id$

I5: $E \rightarrow E * .E$

$E \rightarrow (.E)$

$E \rightarrow .E + E$

$E \rightarrow .E * E$

$E \rightarrow .(E)$

$E \rightarrow .id$

STATE	ACTION						GO TO
	id	+	*	()	\$	E
0	S ₃			S ₂			1
1		S ₄	S ₅			Acc	
2	S ₃		S ₂				6
3		R ₄	R ₄		R ₄	R ₄	
4	S ₃			S ₂			7
5	S ₃			S ₂			8
6		S ₄	S ₅				
7		R ₁	S ₅		R ₁	R ₁	
8		R ₂	R ₂		R ₂	R ₂	
9		R ₃	R ₃		R ₃	R ₃	

I3: $E \rightarrow .id$

I6: $E \rightarrow (E.)$

$E \rightarrow E. + E$

$E \rightarrow E. * E$

I8: $E \rightarrow E * E.$

$E \rightarrow E. + E$

$E \rightarrow E. * E$

I7: $E \rightarrow E + E.$

$E \rightarrow E. + E$

$E \rightarrow E. * E$

I9: $E \rightarrow (E).$

ERROR RECOVERY IN LR PARSING

- An LR parser will detect an error when it consults the parsing action table and find a blank or error entry.
- Errors are never detected by consulting the goto table.
- A canonical LR parser will not make even a single reduction before announcing the error.
- SLR and LALR parsers may make several reductions before detecting an error, but they will never shift an erroneous input symbol onto the stack.

Panic-mode Error Recovery

- We can implement panic-mode error recovery by scanning down the stack until a state s with a goto on a particular nonterminal A is found.
- Zero or more input symbols are then discarded until a symbol a is found that can legitimately follow A .
- The parser then stacks the state $GOTO(s, A)$ and resumes normal parsing.

Phrase-level Recovery

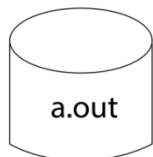
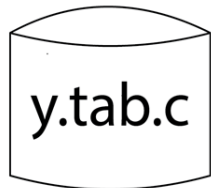
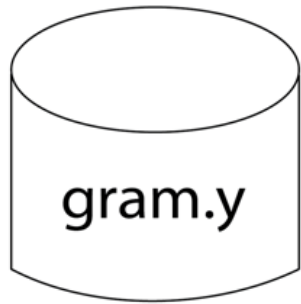
- Phrase-level recovery is implemented by examining each error entry in the LR action table and deciding on the basis of language usage the most likely programmer error that would give rise to that error. An appropriate recovery procedure can then be constructed; presumably the top of the stack and/or first input symbol would be modified in a way deemed appropriate for each error entry.

YACC

- YACC stands for **Yet Another Compiler Compiler**.
- YACC provides a tool to produce a parser for a given grammar.
- YACC is a program designed to compile a LALR (1) grammar.
- It is used to produce the source code of the syntactic analyzer of the language produced by LALR (1) grammar.
- The input of YACC is the rule or grammar and the output is a C program.

- **Input: A CFG- file.y**
- **Output: A parser y.tab.c (yacc)**
- The output file "file.output" contains the parsing tables.
- The file "file.tab.h" contains declarations.
- The parser called the `yyparse ()`.
- Parser expects to use a function called `yylex ()` to get tokens.

The basic operational sequence is as follows:



This file contains the desired grammar in YACC format.

It shows the YACC program.

It is the c source program created by YACC.

C Compiler

Executable file that will parse grammar given in gram.Y